

CS 543

- Final-deliverable



Background

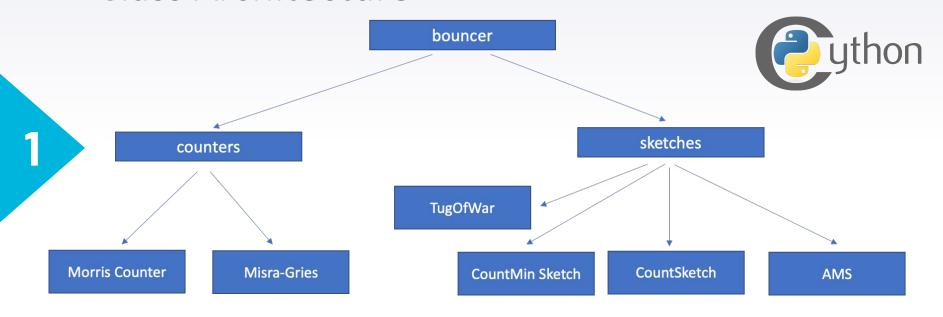


An open source data streaming library for Python, built in C.

Just as a bouncer has to decide who is allowed in a venue and who is not, a data streaming algorithm has to 'decide' which data to 'let in' (use) and which to not in order to approximate the answer.



Class Architecture



Workflow

EDUCATION

- In depth analysis of all methods to be implemented: Jelani Nelson lecture notes
- Extensive c-python api documentation understanding: https://docs.python.org/3/c-a pi/index.html

Research

- Small space K-independent hashing algorithms.
- Translating between C code and python code.
- Engineering decisions about user friendliness vs efficiency.
- Class inheritance and meta-types via C python api.

WORK

- Hashing library to provide user options for which to use per linear sketch.
- Constructors to turn static c struts into python classes.
- Working implementations of Morris, CountMin Sketch, and CountMin





A word about python: Limitations #pragua pack(1)

- Python is a beast!
 Requires a lot of overhead in memory to get anything running.
- Python only has type long for integers, double for floats.
- Everything in python is a pyobject!

```
#pragma pack(1)
typedef struct {
    PyObject_HEAD
    byte* X; // counter
    byte version_flag : 2;
    byte epsilon : 7;
    byte delta : 7;
} Morris;
```

Size of any object instance will at least be the size of the members of its struct!

By default, to start a morris counter instance in python, would require, 16+ bytes!

A word about python : Limitations

- Usability of python library requires access to features inputted.
- An epsilon, delta value by default incur a cost of 8 bytes in C (but actually 16 in Python)!
- These are of course necessary prerequisites to instantiate the object instance.

By storing the Python object version, a string object pointing to either of "Morris, Morris+, Morris++", we also incur at least another 10 bytes of memory by default.

One could find ways to elude this being a parameter, but at the cost of decreasing usability

```
PyGetSetDef get_Morris_sets[] = {
    {"version", /* name */
     (getter) get_version,
     NULL.
     {"epsilon", /* name */
     (getter) get_epsilon,
    NULL, /* doc */
    NULL /* closure */},
     {"delta", /* name */
     (getter) get_delta,
    NULL, /* doc */
    NULL /* closure */},
     {"shape", /* name */
     (getter) get_shape,
     {"raw_counts", /* name */
     (getter) get_raw_counts,
    NULL,
    NULL, /* doc */
    NULL /* closure */},
    {NULL}
```

Requirements and assumptions:



- Requires Python version >= 3.9.9
- Class only works with integer tokens, cannot handle generic types (strings, vectors) as inputs.
- Assumes input domain does not exceed range of 2³1 - 1.

Counters module

```
# Non idealized with random.random() ?
class Morris():
    def __init__(self, epsilon, delta, version = 'morris'):
        assert(epsilon < 0 or epsilon > 1). "epsilon must be set between 0 and 1. non inclusive"
        assert(delta < 0 or delta > 1), "delta must be set between 0 and 1, non inclusive"
        assert(version == 'morris' or version == 'morris+' or version == 'morris++'), "Version must be morris, morris+, or morris++"
        self.delta = delta
        self.epsilon = epsilon
        self.update = lambda x: x + 1 if random.random() <= 1/(2**x) else 0
        self.output = lambda x: (2**x) - 1
        self.version = version
        if self.version == 'morris':
            self.X = 0
        elif self.version == 'morris+':
            self.s = math.ceil(1/(2 * (self.epsilon**2) * self.delta))
            self.X = np.zeros(shape= (self.s, ))
        else: # morris ++
            self.s = math.ceil(3/(2 * (self.epsilon**2)))
            self.t = math.ceil(18 * np.log(1/self.delta))
            self.X = np.zeros(shape= (self.t, self.s,))
```

Init function of Morris counter in python vs in C using the python api.

```
Morris_init(Morris *self, PyObject *args, PyObject *kwds)
   static char *kwlist[] = {"epsilon", "delta", "version", NULL};
   PyObject *version = NULL, *tmp;
   if (!PvArg ParseTupleAndKeywords(args, kwds, "ff0", kwlist, &self->epsilon, &self->delta, &version))
   if((self->epsilon >= 1) || (self->epsilon <= 0) ){
       PyErr_SetString(HyperParameterError, "epsilon must set between 0 and 1");
   if((self->delta >= 1) || (self->delta <= 0)){
       PyErr_SetString(HyperParameterError, "delta must be set between 0 and 1");
   if (!PyUnicode_Check(version)) {
       PyErr_SetString(PyExc_TypeError,
   const char* passed_in_vesion = PyUnicode_DATA(version);
   if(strcmp(passed_in_vesion, "Morris") == 0){
       if ((self->X = (byte*) calloc(1,sizeof(byte))) == NULL){
          PyErr_SetString(MemoryError, "Unable to allocate space, terminating");
       self->version_flag = 0;
   else if( strcmp(passed_in_vesion, "Morris+") == 0){
       self->s = (uint32_t) ceil( 1/((float) 2 * pow(self->epsilon, 2) * self->delta));
       if ((self->X = (byte*) calloc(self->s.sizeof(byte))) == NULL){
          PyErr SetString(MemoryError, "Unable to allocate space, terminating");
       self->version_flag = 1;
   else if(strcmp(passed_in_vesion, "Morris++") == 0 ){
       self->s = (uint32_t) ceil(3/((float) 2 * pow(self->epsilon, 2)));
       self->t = (uint32_t) ceil( 18 * log(1/ (float) self->delta));
       if ((self->X = (byte*) calloc(self->s * self->t, sizeof(byte))) == NULL){
           PyErr_SetString(MemoryError, "Unable to allocate space, terminating");
           return -1:
       self->version flag = 2:
       PyErr_SetString(VersionError, "version must be set to: Morris, Morris+, Morris++");
   tmp = self->version:
   Py INCREF(version);
   self->version = version:
   Pv XDECREF(tmp):
   return 0;
```

Compilation code snippets

```
counters git:(main) × python3 setup.py install
running install
running build
running build_ext
running install_lib
running install_egg_info
Writing /usr/local/lib/python3.9/site-packages/Ben_Badnani-1.0.0-py3.9.egg-info
```

```
ounters > C counters_wrapper.c > Pylnit_counters(void)
     #include "headers/counters_wrapper.h"
     #include "headers/morris counter.h"
     #include "morris counter.c"
     #pragma pack(1)
     PVMODINIT FUNC
     PyInit counters(void)
         PyObject *m;
         if (PyType_Ready(&Morris_type) < 0)</pre>
         m = PyModule Create(&counters module);
         if (m == NULL)
         Py_INCREF(&Morris_type);
         if (PyModule_AddObject(m, "Morris", (PyObject *) &Morris_type) < 0) {
             Py_DECREF(&Morris_type);
             Py_DECREF(m);
         HyperParameterError = PyErr NewException("HyperParameterError.error", NULL, NULL);
         Py_XINCREF(HyperParameterError);
         if (PyModule_AddObject(m, "error", HyperParameterError) < 0) {</pre>
             Pv XDECREF(HyperParameterError);
             Pv CLEAR(HyperParameterError):
             Py_DECREF(&Morris_type);
             Py DECREF(m);
         VersionError = PvErr NewException("VersionError, error", NULL, NULL):
         Py_XINCREF(VersionError);
         if (PyModule_AddObject(m, "error", VersionError) < 0) {</pre>
             Py_XDECREF(VersionError);
             Pv CLEAR(VersionError):
             Py DECREF(&Morris type);
             Py_DECREF(m);
         MemoryError = PyErr NewException("MemoryError.error", NULL, NULL);
         Py XINCREF(MemoryError);
         if (PyModule_AddObject(m, "error", MemoryError) < 0) {
             Pv XDECREF(MemoryError):
             Py_CLEAR(MemoryError);
             Py_DECREF(&Morris_type);
             Py DECREF(m);
         return m;
```

Counters module: results

```
>>> sys.getsizeof(m1)
26
```

```
[>>> from counters import Morris
[>>> m1 = Morris(epsilon = .2, delta = .5, version = "Morris+")
[>>> for i in range(10):
[... m1.update()
[...
[>>> m1.output()
7.639999866485596
```

```
[>>> m1.epsilon 0.200000000298023224
```

```
[>>> m1.delta
0.5
```

```
[>>> m1.version
'Morris+'
```



CountMin module code snippets

```
import numpy as np
import math
from ..utils.utils import nextPrime, LinearSketch
from ..utils.utils import nextPrime

class CountMin(LinearSketch):
    # https://cs-web.bu.edu/faculty/homer/537/talks/SarahAdelBargal_UniversalHashingnotes.pdf , hashing algorithm
    def __init__(self, epsilon, delta, n):
        self.p = nextPrime(math.ceil(2/self.epsilon))
        self.t = math.ceil(math.log2(1/self.delta))

self.random_bits = np.random.choice(range(self.p), size = (self.t, 2))
        self.hash = lambda token,row: ((self.random_bits[row][0]*token) + self.random_bits[row][1]) % self.p

self.count_min_sketch = np.zeros(shape = (self.t, self.p))
```

Init function of CountMin sketch in python vs in C using the python api.

```
tMin init(CountMin *self, PvObject *args, PvObject *kwds) // add n as paramet
hasher = PyUnicode_FromString("CM"); // setting habser default value to "CM"
if (IPyArg_ParseTupleAndKeywords(args, kwds, "ff[0", kwlist, Gepsilon, Edelta, Ghasher)){ // optional argument for hasher, default is "tabulatio PyErr_SetString(MemoryError, "Unable to allocate space, terminating");
PyObject * super args:
if( (super_args = PyTuple_Pack(2, PyFloat_FromDouble((double) epsilon), PyFloat_FromDouble((double) delta))) == NULL){
// super().__init__(epsilon, delta)
iff(LinearSketch init(&self->super, super args, NULL)) != 0){
Py_XDECREF(super_args);
    PyErr SetString(PyExc TypeError.
self->s = (uint32_t) ceil(2/ (float)self->super.epsilon);
self->t = ceil( log(1/(float) self->super.delta));
 const chare passed in vesion = PvUnicode DATA(hasher):
if(stromp(passed in vesion, "tabulation") == 0){
   if( (self->hash_table = (uint32_t*) calloc(self->t, sizeof(uint32_t)) ) == NULL){
       PyErr_SetString(MemoryError, "Unable to allocate space, terminating");
       self->hash_table[i] = rand(); // fill the table with random seed vaalues
   self-shash retriever = Egenerate random bits to
else if( stromp(passed in vesion, "CW") == 8){ // CW for Carter & Wegma
    if( (self->hash_table = generate_random_bits_CW(self->s, self->t, 2)) == NULL){
      PVErr SetString(MemoryError, "Unable to allocate space, terminating"):
    self->hash retriever = &retrieve hash index CM:
   self-shash bit = 1:
else if( strcmp(passed_in_vesion, "mult-shift") == 0){ // CW for Carter & Megma
   if( (self->hash_table = generate_random_bits_D(self->s, self->t, 2)) == NULL){
        PyErr_SetString(MemoryError, "Unable to allocate space, terminating");
   self->hash retriever = &retrieve hash index D:
   self->hash bit = 2:
if ((self->super.X = (int*) calloc(self->s * self->t.sizeof(int))) == NULL){ // can use uint32 t pointer since i
   PyErr SetString(MemoryError, "Unable to allocate space, terminating"):
self->hasher = hasher:
if( (self->shape = PyTuple_Pack(2, PyLong_FromUnsignedLong((unsigned long) self->t), PyLong_FromUnsignedLong((unsigned long) self->s))) == NULL){
```

CountMin module: | >>> import sys | >>> sys.getsizeof(c1) results

```
[>>> from sketches import CountMin
[>>> c1 = CountMin(epsilon = .2, delta = .5, hasher = "CW")
[>>> sample_token_stream = [ (1, 1), (2,1), (1, -1), (2,-1), (1,2)]
[>>> for token,count in sample_token_stream:
        c1.update(token, count)
[>>> c1.query(1)
[>>> c1.query(2)
```

```
>>> c1.delta
0.5
>>> c1.epsilon
0.20000000298023224
>>> c1.shape
```

>>> c1.hasher



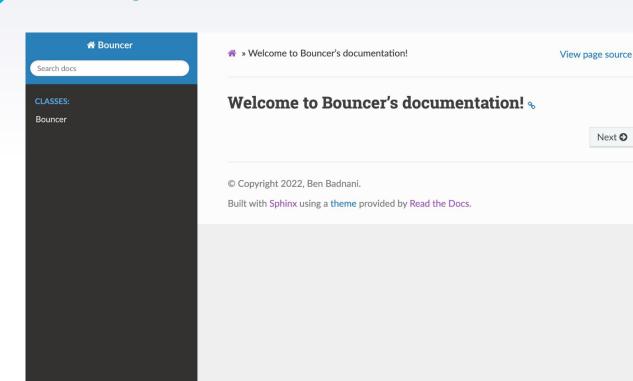
Hash library

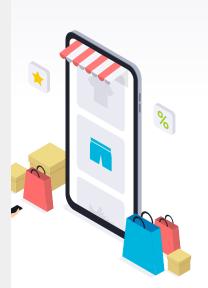
```
// M. DIETZFELBINGER, Universal hashing and k—wise independent random variables via integer arithmetic without pr
2 independent hashing M. DIETZFELBINGER.
uint32 t* generate random bits D(uint32 t num hash buckets, uint32 t instantiations, uint8 t independence degree)
   // assumes input can be represented with at most 32 bits.
   uint64 t i;
   uint32_t* hash_table;
   if ((hash_table = (uint32_t*) calloc(instantiations * 2,sizeof(uint32_t))) == NULL){
       return NULL;
   for(i = 0; i < instantiations * independence degree; i ++){</pre>
       hash table[i] = rand(): // pick a random number in 2^{input bit size}, 2^32
   return hash_table;
uint32_t retrieve_hash_index_D(uint32_t num_hash_buckets, int token, int* rand_bits) // pointer into the table of
   uint32_t a, b; // to prevent overflow
   a = rand_bits[0];
   b = rand bits[1];
   uint16 t hash bits = log2(num hash buckets);
   return (a * token + b) >> (32 - hash_bits);
```

Hash library

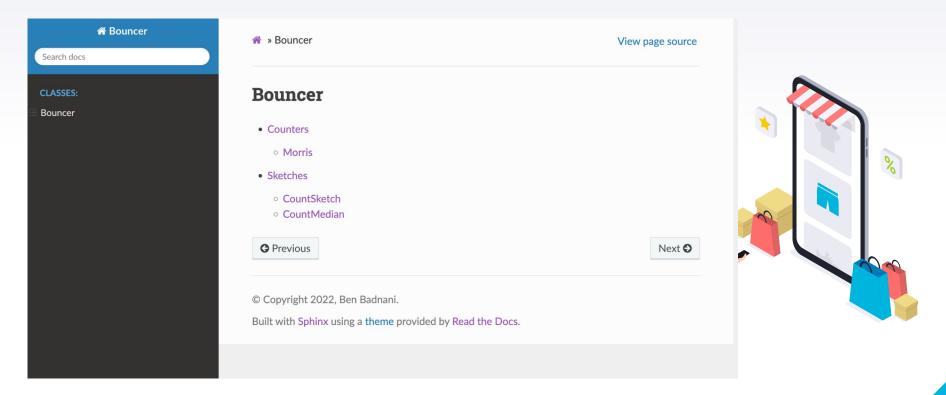
```
M. DIETZFELBINGER, Universal hashing and k-wise independent random variables via integer arithmetic without pr
2 independent hashing M. DIETZFELBINGER
/********
                       uint32_t* generate_rand
   // assumes input ca
                       uint32 t* generate random bits CW(uint32 t num hash buckets, uint32 t instantiations, uint8 t independence degree) // number of random
   uint64 t i;
   uint32 t* hash tabl
                          uint64 t i:
   if ((hash_table = (
       return NULL;
                          uint32 t* hash table;
                          if ((hash_table = (uint32_t*) calloc(instantiations * independence_degree,sizeof(uint32_t))) == NULL){
   for(i = 0; i < inst
                              return NULL:
       hash table[i] =
                          for(i = 0: i < instantiations * independence degree: i ++){</pre>
                              hash table[i] = rand() / (RAND_MAX / num hash buckets + 1); // generate random number between 0 and prime for all indices
   return hash_table;
                          return hash_table;
uint32_t retrieve_hash_
                       uint32 t retrieve hash index CW(uint32 t num hash buckets, int token, int* rand bits) // pointer into the table of random bits
   uint32_t a, b; // {
   a = rand_bits[0];
                          uint64_t hash_val = 0; // to prevent overflow
   b = rand bits[1];
                          for(uint32 t i = 0; i < num hash buckets; i ++){</pre>
                              hash_val += pow(token, i) * rand_bits[i];
   uint16 t hash bits
   return (a * token +
                          hash val = hash val% num_hash_buckets; // modulus the number of buckets
                          return (uint32_t) hash_val;
```

Sample documentation

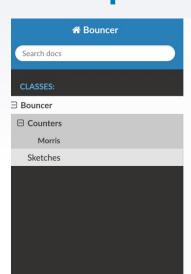




Sample documentation



Sample documentation



* » Bouncer » Counters » Morris

View page source

Morris

The Morris counter is one of the first streaming algorithms ever discovered. For a stream of n tokens, the Morris counter seeks to approximate the number of items in the stream in only $O(\log n)$ bits of memory. Because the Morris counter acts as an unbiased estimator, we can approximate n up to value 2^{256} , using just one byte of memory for the counter. The algorithm works strictly on a vanilla model, meaning it can only record event insertions and does not allow for deletions.

class bouncer.counters.Morris(version, epsilon, delta)

Parameters

version: {"Morris", "Morris+", "Morris++"}, default="Morris"

Specify the type of Morris counter.

- "Morris" : One 8-bit Morris counter.
- "Morris+": $s = \left\lceil \frac{1}{\epsilon^2 \delta} \right\rceil$ "Morris" counters.
- "Morris++": $t=\lceil \frac{18}{\log \delta} \rceil$ "Morris+" counters, where $s=\lceil \frac{3}{2\epsilon^2} \rceil$.

epsilon: float, range=(0,1)

Accepted error range of true count. Only implemented for 'Morris+', 'Morris++'.

delta: float, range=(0,1)

Probability of exceeding epsilon error range. Only implemented for 'Morris+', 'Morris++'.



Examples

```
>> from bouncer.counters import Morris
>> m = Morris(version="Morris")
>> for i in range(10):
      m_update()
>>
>> m.output()
>> 15
>> m.shape
>> (1,)
>> m.raw_counts
>> [4]
>>
>> m1 = Morris(version="Morris+", epsilon = .2, delta = .5)
>> for i in range(10):
      m1.update()
...
>>
>> m1.output()
>> 7.639999866485596
>> m1.shape
>> (1, 25)
>> m1.raw_counts
>> [2, 2, 3, 3, 3, 2, 3, 4, 3, 2, 3, 3, 2, 3, 3, 3, 3, 3, 2, 4, 3, 3, 4, 4, 4]
>> m2 = Morris(version="Morris++", epsilon = .2, delta = .5)
>> for i in range(10):
       m2.update()
>>
>> m2.output()
>> 10.894737243652344
>> m2.shape
>> (13, 38)
```



Examples

```
>> from bouncer.counters import Morris
>> m = Morris(version="Morris")
>> for i in range(10):
      m_update()
>> m.output()
>> 15
>> m.shape
>> (1,)
>> m.raw_counts
>> [4]
>>
>> m1 = Morris(version="Morris+", epsilon = .2, delta = .5)
>> for i in range(10):
      m1.update()
>>
>> m1.output()
>> 7.639999866485596
>> m1.shape
>> (1, 25)
>> m1.raw counts
>> [2, 2, 3, 3, 3, 2, 3, 4, 3, 2, 3, 3, 2, 3
>> m2 = Morris(version="Morris++", epsilon =
>> for i in range(10):
       m2.update()
>> m2.output()
>> 10.894737243652344
>> m2.shape
>> (13, 38)
```



Note

This implementation requires 26 bytes of overhead per instantiation. This is due to the overhead of PyObject HEAD and other python fields required for all python object allocations.

Analysis and proof of correctness of the bounds can be found in Jelani Nelson's lecture notes under chapter 2.1.2: https://www.sketchingbigdata.org/fall20/lec/notes.pdf





Credits and Acknowledgements

None of this would be possible without the following people:

- Krzysztof Onak
- Nadya Voronova
- Jelani Nelson
- Amit Chakrabarti
- My roomates Ben Blackman and Leor Lavi for the logo and name.



Library can be found at:

https://github.com/KeyAleph/Bouncer

Note: library is currently private

Sources:

- Carter, Larry; Wegman, Mark N. (1979). "Universal Classes of Hash Functions". Journal of Computer a System Sciences. 18 (2): 143–154. doi:10.1016/0022-0000(79)90044-8. Conference version in STOC'77. M. Dietzfelbinger. Universal hashing and k-wise pendent random via la Britan and k-wise and service with the state of the STAGE LARGE AND ADDITIONAL PROPERTY.

- arithmetic without primes. In Proc. 13th STACS, LNCS 1046, pages 569–580, 1996.

 Pătrașcu, Mihai; Thorup, Mikkel (2012), "The power of simple tabulation hashing", Journal of the ACM, 59 (3): Art. 14, arXiv:1011.5200, doi:10.1145/2220357.2220361, MR 2946218.

What's Next?

What's next?

- Automatic Documentation with sphinx.
- Half-precision floating-point to decrease overhead!
- Implementation of Galois fields in C for universal hashing algorithms.
- Nisan's Pseudorandom Number Generator for derandomization and less random bit space usage!
- Add more algorithms!



THANKS!

Any questions?

